## MTH 211, Math for Architects, Exam I, Spring 2014

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## Each question $\mathbf{1 0}$ points, total points $=\mathbf{9 0}$

QUESTION 1. Draw a reasonable line segment and call it $A B$. Find the mid-point of AB and call it $M$. Draw a semi-circle centered at $M$ with radius $|M B|$ (To construct your semi-circle, just take the upper-half of the circle centered at M with radius IMBI$)$. Now construct a rectangle $E L F D$ where $E, L$ are points on AB (call EL the width of the rectangle), $F, D$ are points on the semi-circle you constructed (Call $L F$ the length of the rectangle) such that $|L F|=1.5|E L|+|M K| / 3$, where $M K$ is perpendicular to $A B$ at $M$ and intersects the semi-circle at the point $K$. STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

QUESTION 2. Draw a reasonable line segment and call it $A B$. Construct a point $C$ on the line segment $A B$ such that $\frac{|A C|+|C B|}{|A C|}=0.5 \frac{|A C|}{|C B|}$. What is the numerical value of this ratio? STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

QUESTION 3. Given $a_{0}=1, a_{1}=1$, and $a_{n}=4 a_{n-1}+5 a_{n-2}$ for each $n \geq 2$. First calculate $a_{2}, a_{3}$. Find a general formula for $a_{n}$. Now use the formula to find $a_{2}, a_{3}$, and $a_{7}$.

QUESTION 4. a) Can we construct a regular 18-gon? Explain.
b) Can we construct a 54-degrees angle? EXPLAIN
c)Can we construct a regular 34-gon? EXPLAIN
d) Can we construct an 80-degree angle? Explain

QUESTION 5. Draw a line segment $A B$. Now divide $A B$ into 3 segments, say $S_{1}, S_{2}, S_{3}$ such that $\left|S_{1}\right|=\left|S_{2}\right|$ and $\left|S_{3}\right|=\sqrt{2}\left|S_{1}\right|$.

QUESTION 6. Construct a pentagon inside a circle. Now use the constructed pentagon in order to construct a regular 15-gon. STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

QUESTION 7. You are given a line segment of length 1 cm . Draw a line segments $A B$. Now construct two line segments, say $C D$ and $E F$ such that $|C D|>|A B|$ and $|A B|=|C D||E F|$. STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

QUESTION 8. You are given a line segments, say $A B$. YOU ARE NOT ALLOWED to use a marked ruler. Construct a line segment of length $\frac{|A B|}{\sqrt{3}}$. STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

QUESTION 9. You are given a line segment of length $x>1$ and a line segment of length 1 cm . Construct a line segment of length $\sqrt{\sqrt{5} x^{3}-0.5 x^{3}}$. STATE the steps CLEARLY and try to be BRIEF to the point. Illustrate the steps by diagrams.

## Faculty information

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